

How to do cross-sectional network analyses?

A 6,5-minute tutorial of Pnet, utilizing Exponential Random Graph Models (ERGMs, *p**)

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Exponential Random Graph Models

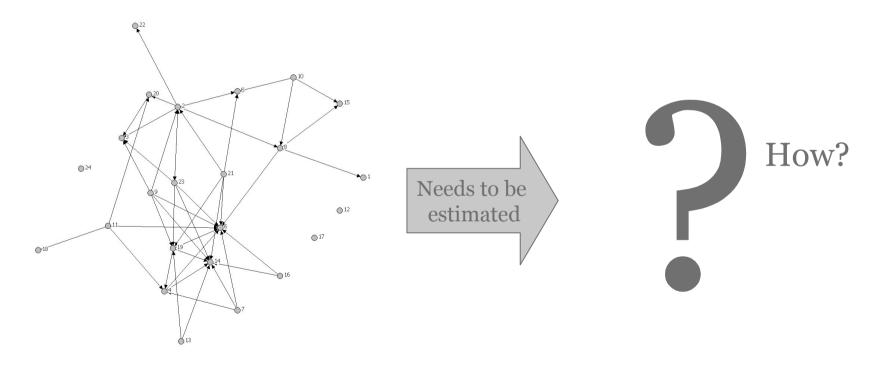
- Analyze complete networks
- > They include random effects, capturing the *irregularity* of everyday life
- > Tie formation is assumed to depend on others.
 - For example, sharing many friends makes the establishment of a friendship more likely
- > Homogeneity is assumed, which means that network parameters are the same for all actors in the network.



Network Analyses = Modeling networks

Observed network

Estimated network

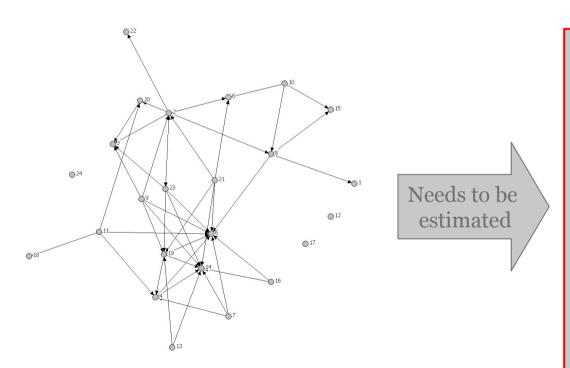




Network Analyses = Modeling networks

Observed network

Estimated network



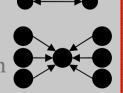
By means of **configurations**:

These are subsets of actors and ties between them:

e.g.,

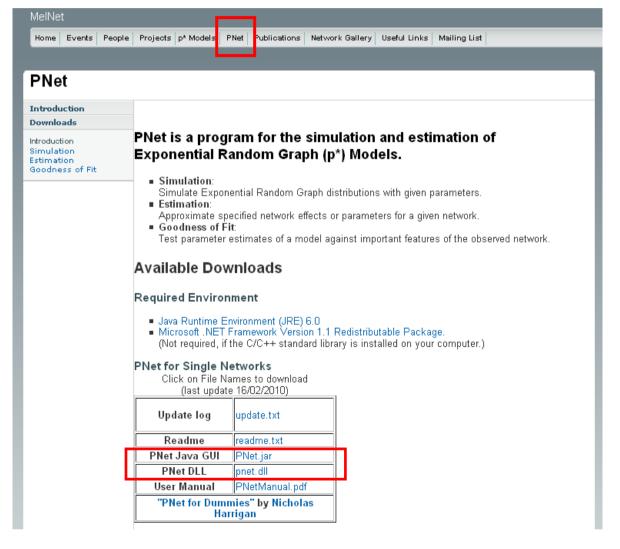
-Reciprocity

- Indegree distribution



Step 1:

- Download the program Pnet
- » sna.unimelb.edu.au/



Step 2:

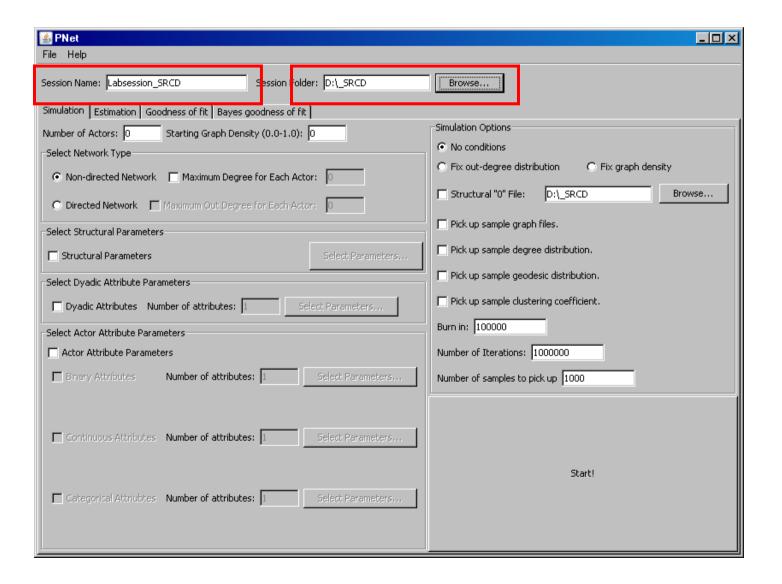
> Open the program!

<u>≰</u> PNet	_ D X
File Help	
Session Name: Session Folder:	Browse
Simulation Estimation Goodness of fit Bayes goodness of fit	
Number of Actors: 0 Starting Graph Density (0.0-1.0): 0	Simulation Options
Select Network Type	No conditions
Non-directed Network	C Fix out-degree distribution C Fix graph density
C Directed Network Maximum Out: Degree for Each Actor: 0	Structural "0" File: Browse
Select Structural Parameters	Pick up sample graph files.
■ Structural Parameters	Pick up sample degree distribution.
Select Dyadic Attribute Parameters	Pick up sample geodesic distribution.
Dyadic Attributes Number of attributes: 1 Select Parameters	Pick up sample clustering coefficient.
Select Actor Attribute Parameters	Burn in: 100000
Actor Attribute Parameters	Number of Iterations: 1000000
☐ Binary Attributes Number of attributes: 1 Select Parameters	Number of samples to pick up 1000
Continuous Attributes Number of attributes: 1 Select Parameters	
	Start!
Categorical Attriubtes Number of attributes: 1 Select Parameters	

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Step 3:

> Provide session name and select folder with the data





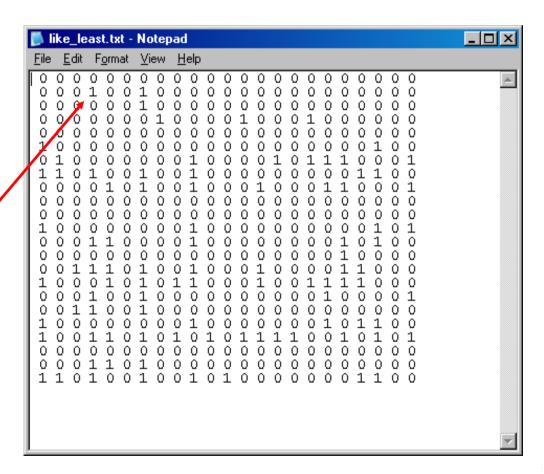
Step 4:

> Press estimation, provide number of children in the classroom, and select the network file

PNet	_ D X
File Help	
Session Name: Labsession_SRCD Session Folder: D:_SRCD Simulation Estimation Soodness of fit Bayes goodness of fit	Browse
Number of Actors: 23 Network File: D:_SRCD\like_least.txt Browse	Estimation Options No conditions
Select Network Type	C Fix out-degree distribution C Fix graph density
Non-directed Network	Structural "0" File: D:_SRCD Browse
Directed Network	Number of Subphases: 5
Select Structural Parameters	Gaining Factor (a-value): 0.01
Select Parameters Select Parameters	Multiplication Factor: 10
Select Dyadic Attribute Parameters	Number of Iterations in Phase 3: 500
Dyadic Attributes Number of attributes: 1 Select Parameters	Max. Number of Estimation Runs: 1
Select Actor Attribute Parameters	☐ Do GOF @ model convergence
Actor Attribute Parameters	
Binary Attributes Number of attributes: 1 Select Parameters	Start!
Continuous Attributes Number of attributes: 1 Select Parameters	
Categorical Attriubtes Number of attributes: 1 Select Parameters	Update!

Network file

- A matrix with rows and columns equal to the number of children in the classrooms
- > "1" indicate a tie, "o" indicate no tie.
- For example, child 2nominates child 4



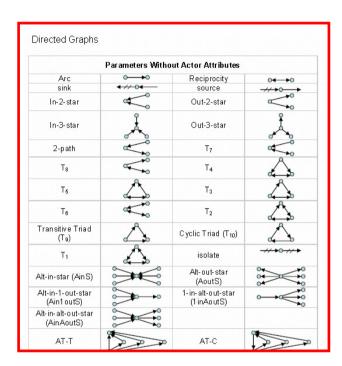


Step 5:

> Select the structural parameters

<u> </u>	_
File Help	
Session Name: Labsession_SRCD Session Folder: D:_SRCD	Browse
Simulation Estimation Goodness of fit Bayes goodness of fit	
Number of Actors: 23 Network File: D:_SRCD\like_least.txt Browse	Estimation Options No conditions
Select Network Type	C Fix out-degree distribution C Fix graph density
○ Non-directed Network	Structural "0" File: D:_SRCD Browse
Directed Network	Number of Subphases: 5
Select Structural Parameters	Gaining Factor (a-value): 0.01
▼ Structural Parameters Select Parameters	Multiplication Factor: 10
Select Dyadic Attribute Parameters	Number of Iterations in Phase 3: 500
Dyadic Attributes Number of attributes: 1 Select Parameters	Max. Number of Estimation Runs: 1
Select Actor Attribute Parameters	Do GOF @ model convergence
Actor Attribute Parameters	
☐ Binary Attributes Number of attributes: 1 Select Parameters	
	Start!
Continuous Attributes Number of attributes: 1 Select Parameters	
Categorical Attriubtes Number of attributes: 1 Select Parameters	Update!

Parameters



Explanations of the meaning of the parameters can be found in the PNetmanual (see PNet-website)

🚣 Structural Parameter Selection	
Markov Parameters	High-Order Parameters
☐ Arc □	☐ AinS
Reciprocity 0	Aout5 lambda: 2
☐ In-2-star □	AinS-2nd lambda: 2
Out-2-star	AoutS-2nd 0 lambda: 2
☐ In-3-star □	AinAout5 lambda: 2
Out-3-star	Ain1out5 lambda: 2
2-path 0	☐ 1inAoutS ☐ lambda: 2
	AT-T Iambda: 2
Transitive-Triad 0	AT-C lambda: 2
Cyclic-Triad 0	AT-D ambda: 2
□ T1 0	AT-U lambda: 2
□ T2 0	AT-TD lambda: 2
□ T3 0	AT-TU ambda: 2
□ T4 □	AT-DU 0 lambda: 2
□ τ5 □	AT-TDU lambda: 2
<u></u> ⊤6 □	A2P-T 0 lambda: 2
	A2P-D lambda: 2
T8 0	A2P-U 0 lambda: 2
☐ Sink □	A2P-TD 0 lambda: 2
	A2P-TU 0 lambda: 2
Source 0	A2P-DU 0 lambda: 2
☐ Isolates □	A2P-TDU lambda: 2
J'Clear All	Select All OK



Step 6:

> Fix the graph density, increase the multiplication factor (>50), and set the estimation runs to 10

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File Help	
Session Name: Labsession_SRCD Session Folder: D:_SRCD	Browse
Simulation Estimation Goodness of fit Bayes goodness of fit	
Number of Actors: 23 Network File: D:_SRCD\like_least.txt Browse	Estimation Options No conditions
Select Network Type	○ Fix out-degree distribution
○ Non-directed Network	☐ Structural "0" File: D:_SRCD Browse
⊙ Directed Network	Number of Subphases: 5
Select Structural Parameters	Gaining Factor (a-value): 0.01
Structural Parameters Select Parameters	Multiplication Factor: 75
Select Dyadic Attribute Parameters	Number of Iterations in Phase 3: 500
Dyadic Attributes Number of attributes: 1 Select Parameters	Max. Number of Estimation Runs: 10
Select Actor Attribute Parameters	□ Do GOF @ model convergence
Actor Attribute Parameters	
☐ Binary Attributes Number of attributes: 1 Select Parameters	
	Start!
Continuous Attributes Number of attributes: 1 Select Parameters	
Categorical Attriubtes Number of attributes: 1 Select Parameters	Update!
	2,2333

Step 7:

> Request a GoF (Goodness of Fit)

<u> </u>	_ D ×
File Help	
Session Name: Labsession_SRCD Session Folder: D:_SRCD	Browse
Simulation Estimation Goodness of fit Bayes goodness of fit	
Number of Actors: 23 Network File: D:_SRCD\like_least.txt Browse	Estimation Options O No conditions
Select Network Type	C Fix out-degree distribution
○ Non-directed Network	☐ Structural "0" File: D:_SRCD Browse
Directed Network	Number of Subphases: 5
Select Structural Parameters	Gaining Factor (a-value): 0.01
Structural Parameters Select Parameters	Multiplication Factor: 75
Select Dyadic Attribute Parameters	Number of Iterations in Phase 3: 500
Dyadic Attributes Number of attributes: 1 Select Parameters	Max. Number of Estimation Runs: 10
Select Actor Attribute Parameters	☐ Do GOF @ model convergence
Actor Attribute Parameters	
Binary Attributes Number of attributes: 1 Select Parameters	Start!
Continuous Attributes Number of attributes: 1 Select Parameters	
Categorical Attriubtes Number of attributes: 1 Select Parameters	Update!



Goodness of fit

- Compares parameters of observed networks with estimated parameters
- > Convergence t-ratio =

(Observed network - Mean simulated networks)
Standard error simulated networks

The smaller the ratio, the less difference between estimated and observed parameters!

Estimated (<0.10) & unestimated (<2.00) parameters

Step 8:

> Press Start!

<u>≨</u> PNet	_ ×
File Help	
Session Name: Labsession_SRCD Session Folder: D:_SRCD	Browse
Simulation Estimation Goodness of fit Bayes goodness of fit	
Number of Actors: 23 Network File: D:_SRCD\like_least.txt Browse	Estimation Options C No conditions
Select Network Type	C Fix out-degree distribution
C Non-directed Network Maximum Degree for Each Actor: 0	Structural "0" File: D:_SRCD Browse
© Directed Network	Number of Subphases: 5
Select Structural Parameters	Gaining Factor (a-value): 0.01
Structural Parameters Select Parameters	Multiplication Factor: 75
Select Dyadic Attribute Parameters	Number of Iterations in Phase 3: 500
Dyadic Attributes Number of attributes: 1 Select Parameters	Max. Number of Estimation Runs: 10
Select Actor Attribute Parameters	☐ Do GOF @ model convergence
Actor Attribute Parameters	
☐ Binary Attributes Number of attributes: 1 Select Parameters	
	Start!
Continuous Attributes Number of attributes: 1 Select Parameters	
Categorical Attriubtes Number of attributes: 1 Select Parameters	Update!

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Step 9:

stimation Labsession SRCD.txt - Notepad

Number of estimation runs = 10

STOCHASTIC APPROXIMATION RUN 1

starting parameters:0.000000

STOCHASTIC ESTIMATION FOR NETWORK Labsession_SRCD

Number of sub-phases in estimation (phase 2) = 5 starting a-value in estimation (phase 2) = 0.010000 Multiplication factor for estimation (phase 2) = 75 Number of steps in final simulation (phase 3) = 500

original statistics:13.000000 115.798828

num of steps = 13
num of iterations in each step = 5951.807851

Phase1 started with the following setup:

END PHASE1 parameter:0.000000 0.000000

mean statistics in phase1:7.384615

File Edit Format View Help

ESTIMATION SETTINGS

a = 0.010000

Phase 2 started

- > Inspect your results
- > T-ratios smaller than 0.10 reflect good model convergence.

```
mean statistics in phase3:12.976600 115.648438

Estimation Result for Network SUMMARY (parameter, standard error, t-statistics)
NOTE: t-statistics = (observation - sample mean)/standard error

effects estimates stdern t-ratio
reciprocity 0.680335 0.30431 0.00921 *
Ains(2.00) 1.298692 0.28083 0.04216 *
```

- > In this classroom, there was a significant number of reciprocal nominations
- Some children attracted many nominations (alternating-in-star)

```
Subphase 2 has gone up to 65 steps
Parameter after Subphase 2: 0.63490
                                         1.28492
Subphase 3 started with a valued 0.002500
Subphase 3 has gone up to 344 steps
Parameter after Subphase 3: 0.67043
                                         1.31073
Subphase 4 started with a valued 0.001250
Subphase 4 has gone up to 563 steps
Parameter after Subphase 4: 0.68033
END PHASE2 parameter:0.680335 1.298692
Phase3 started with the following setup:
num of steps = 500
num of iterations in each step = 5951.807851
mean statistics in phase3:12.976000
Estimation Result for Network SUMMARY (parameter, standard error, t-statistics)
NOTE: t-statistics = (observation - sample mean)/standard error
leffects estimates
                       stderr t-ratio
                0.680335
                                0.30431 0.00921 *
 eciprocity
                1.298692
                                0.28083 0.04216 *
Estimated Covariance Matrix
0.147694
                0.006536
0.006536
                0.078866
```

105.405048



Step 10:

- > Inspect model convergence
- All t-ratios should be smaller than 2 to reflect good model convergence.

- This model is not good,
 many parameters are underor overestimated
- The solution would be to include more parameters

	D gof_Labsession_SRCD.txt - Notepad	_
	File Edit Format View Help	
	t-statistics = (observation - sample mean)/standard deviation	▲
# P	effects observed mean stddev t-ratio arc 93 93.000 0.000 -1.#IO reciprocity 13 13.171 2.634 -0.065 2-in-star 251 226.418 19.506 1.260 2-out-star 285 176.287 10.393 10.460 3-in-star 494 366.067 77.187 1.657 3-out-star 654 208.319 37.985 11.733 path2 318 361.838 21.181 -2.070 T1 0 0.457 0.723 -0.632 T2 7 8.044 5.699 -0.183 T3 26 23.525 8.773 0.282 T4 13 14.407 5.196 -0.271 T5 26 11.792 4.685 3.033 T6 24 17.471 7.960 0.820 T7 121 126.320 27.901 -0.191 T8 154 100.992 24.138 2.196 T9(030T) 117 83.306 12.687 2.656 T1(030C) 19 22.664 5.485 -0.668 sink 5 0.181 0.415 11.606	
2-ou 3-in 3-ou path T1 T2 T3 T4 T5 T6 T7 T8	n-star 251 226.418 19.506 1.260 ut-star 285 176.287 10.393 10.460 n-star 494 366.067 77.187 1.657 ut-star 654 208.319 37.985 11.733	
	A2P-DU(2.00) 176.176 161.620 5.146 2.829 A2P-TDU(2.00) 200.706 206.536 5.892 -0.990 Std Dev in-degree dist 3.155 2.760 0.320 1.235 Skew in-degree dist 0.535 0.090 0.272 1.634 Std Dev out-degree dist 0.670 0.234 0.399 1.092 Corrcoef in-out-degree dists -0.122 0.106 0.201 -1.138 Global Clustering Cto 0.205 0.236 0.033 -0.934 Global Clustering Cti 0.233 0.184 0.023 2.145 Global Clustering Ctm 0.368 0.230 0.031 4.442 Global Clustering Ctm 0.368 0.230 0.031 4.442 Global Clustering AKC-T 0.332 0.228 0.027 3.795 Global Clustering AKC-D 0.213 0.234 0.029 -0.720 Global Clustering AKC-D 0.213 0.234 0.029 -0.720 Global Clustering AKC-D 0.213 0.234 0.029 -0.720 Global Clustering AKC-U 0.214 0.184 0.019 1.566 Global Clustering AKC-C 0.183 0.187 0.032 -0.114 ACCEPTANCE RATE: 0.6517 SAMPLE GEODESIC DISTRIBUTION	



Need help??

- > See: sna.unimelb.edu.au/
- See the PNet manual,
 or the PNet for Dummies
 guide
- Or contact us:g.e.huitsing@rug.nl

PNet

Program for the Simulation and Estimation of Exponential Random Graph (p*) Models

USER MANUAL

Peng Wang

Garry Robins

Philippa Pattison

Department of Psychology School of Behavioural Science University of Melbourne Australia

September, 2009

PNet for Dummies

An introduction to estimating exponential random graph (p*) models with PNet

Version 1.04

Nicholas Harrigan

To download the latest copy of this manual go to: http://www.ana.unimeib.edu.au/onet/pnet.html#download



Now you are also qualified to perform ERGMs!

www.gmw.rug.nl/~veenstra/