

The evolution of costly mate choice against segregation distorters

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The evolution of female preference for male genetic quality remains a controversial topic in sexual selection research. One wellknown problem, known as the lek paradox, lies in understanding how variation in genetic quality is maintained in spite of natural selection and sexual selection against low-quality alleles. Here, we theoretically investigate a scenario where females pay a direct fitness cost to avoid males carrying an autosomal segregation distorter. We show that preference evolution is greatly facilitated under such circumstances. Because the distorter is transmitted in a non-Mendelian fashion, it can be maintained in the population despite directional sexual selection. The preference helps females avoid fitness costs associated with the distorter. Interestingly, we find that preference evolution is limited if the choice allele induces a very strong preference or if distortion is very strong. Moreover, the preference can only persist in the presence of a signal that reliably indicates a male's distorter genotype. Hence, even in a system where the lek paradox does not play a major role, costly preferences can only spread under specific circumstances. We discuss the importance of distorter systems for the evolution of costly female choice and potential implications for the use of artificial distorters in pest control.

KEY WORDS: Lek paradox mate choice, models/simulations, meiotic drive, selection-sexual, segregation distortion.

Female mate choice is likely to be associated with fitness costs, such as the time and energy associated with searching for suitable mates and the resources allocated to the sensory machinery to discriminate among males (Andersson 1994). Female choosiness will therefore only evolve if these costs are compensated by benefits. A popular argument proposes that choosiness confers genetic benefits to the offspring of choosy females, since such females will tend to mate with males of higher genetic quality. However, this line of argumentation has to face a fascinating problem, generally known as the "lek paradox" (Kirkpatrick and Ryan 1991). Directional sexual selection through female choice will, in combination with natural selection, rapidly remove low-quality alleles from the population. If this occurs, very little variation in genetic quality will remain. As a consequence, choosiness has not much of an effect and the benefits of choosiness become negligible. This

raises a simple yet puzzling question: why do females continue to be choosy if this choosiness depletes genetic variation in the male traits, which in turn is a prerequisite for the evolution of female choice?

Any resolution of this problem requires an explanation of how male trait variation persists despite directional sexual selection imposed by female choice. Several such explanations have been provided elsewhere (Pomiankowski et al. 1991; Pomiankowski and Moller 1995; Kotiaho et al. 2001; Tomkins et al. 2004). Here, we want to theoretically examine the potential of segregation distorter systems to facilitate the evolution of costly female mate choice. By distorting transmission ratio in their own favor, distorters may act as generators of allelic variation in the male trait. In consequence, genetic variance in the trait may be maintained despite directional sexual selection. Moreover,

distorters are usually associated with substantial fitness costs to their carriers (Burt and Trivers 2006). Females may hence protect their offspring from detrimental fitness effects by avoiding fertilization with distorter-carrying males.

Connections between sexual selection and segregation distorters have been suggested by many empirical studies (see Wedell (2013) for a recent review). Female choice may happen both at a pre- and postmating stage. Premating preferences for an absence of distorters or for drive suppressors have been reported in stalk-eyed flies (Wilkinson et al. 1998; Cotton et al. 2014), house mice (Lenington et al. 1992), and Drosophila paulistorum (Miller et al. 2010). A larger body of work highlights the importance of sexual selective processes at the postmating stage. As a direct consequence of segregation distortion, distorter carrying males are typically weak sperm competitors (Zeh and Zeh 1997). Hence, female multiple mating (polyandry) has been proposed as a possible female counterstrategy against distorters (Haig and Bergstrom 1995). Polyandry can result in systematic deviations from random fertilization assumptions. It has thus been considered a form of indirect female mate choice (Brooks and Griffith 2010). Evidence for distorters favoring polyandry has been found in Drosophila simulans (Atlan et al. 2004), Drosophila pseudoobscura (Price et al. 2008), and the butterfly Hypolimnas bolina (Charlat et al. 2007).

Given this considerable body of empirical evidence, surprisingly few studies have investigated the theoretical implications of segregation distortion on mating preferences. However, sexual selection models are complicated considerably when a distorter is added. While most population genetics models of sexual selection are framed in terms of haploids (Kuijper et al. 2012), segregation distortion requires the analysis of diploid organisms, which makes analysis much more intricate (Greenspoon and Otto 2009). Most previously published models focus on the interplay between female choice and sex-linked distorters. Motivated by the stalk-eyed fly system (Wilkinson et al. 1998), two models investigated possible interactions between female choice and a sex-linked distorter. Reinhold et al. (1999) consider female choice for a distortion suppressor. The model suggests that, unexpectedly, female preferences in favor of a distortion suppressor is always selected against. Lande and Wilkinson (1999) chose a more direct approach and analyzed a situation where females choose a male trait (eye-span in this particular example) that indicates the absence of the distorter allele. They found that female preference for the trait can evolve, but only if the trait is perfectly coupled with the distorter. Even a small rate of recombination between a trait locus and the distorter locus will prevent the evolution of female choice. Randerson et al. (2000) investigated the evolution of costly male mate choice in the butterfly Acraea encedon infected with malekilling Wolbachia. Because the male killer causes a strong female bias in infected populations, sex-roles appear reversed and males

Table 1. Overview over the three loci and the parameters used in the model. Sex symbol in brackets indicate the sex in which the given property is expressed.

Trait locus <i>T</i> Viability ()		$T_0 T_0$	T_0T_1 $1 - h_t c_t$	T_1T_1 $1-c_t$
Preference locus P		P_0P_0	P_0P_1	P_1P_1
Preferences ()	T_0T_0	1	1	1
, , , , , , , , , , , , , , , , , , ,	T_0T_1	1	$1 + h_a h_p a$	$1 + h_a a$
	T_1T_1	1	$1 + h_p a$	1+a
Viability ()		1	$1 - c_p/2$	$1 - c_p$
Segregation		S_0S_0	S_0S_1	S_1S_1
locus S				
either:		1	1	0
Viability ()				
or: Fertility ()		1	1	0
Segregation ratio ()		0	d	1

should avoid infected females. The model confirms this expectation, as long as males do not perfectly discriminate between infected and uninfected females. In this case, costly male choice can stably persist. If males make no mistakes, costly male choice succumbs to its own success, since by effectively removing the male killer from the population, it also removes the benefits of being choosy.

Here, we investigate a model for the evolution of a costly female preference in the presence of an autosomal segregation distorter. In particular, we address the following questions: (1) Can the presence of an autosomal distorter facilitate the spread of a costly female preference for Mendelian segregation (i.e. distorter-free males)? (2) What levels of preference cost, preference and distortion strength allow for the evolution of costly female preferences? (3) How does recombination between a male sexual signal and a distorter affect evolutionary outcomes?

The Model

Our model follows the standard set-up of population genetic models of sexual selection (Kuijper et al. 2012) and adds segregation distortion as an additional factor. We consider diploid organisms and three autosomal loci: a trait locus T encoding for a sexual ornament in males; a preference locus P affecting female choice for the ornament; and a distorter locus S affecting Mendelian segregation in males. The following two alleles segregate at each of the three loci (see Table 1 for an overview).

• The trait locus (T) is expressed in males only and encodes a trait that is subject to both viability and sexual selection. It contains alleles T_0 and T_1 (at frequencies t_0 and t_1 , respectively), where

allele T_1 induces a viability disadvantage but can be the target of female preference.

- The preference locus (P) is expressed in females only and determines her relative tendency to mate with males of the three possible genotypes at the T locus. It contains alleles P_0 and P_1 (at allele frequencies p_0 and p_1 , respectively), where P_1 is defined as the allele that induces female preference. The expression of female preference is associated with a fixed viability cost.
- The distorter locus (S) contains alleles S_0 and S_1 (at allele frequencies s_0 and s_1 , respectively). The proportion of distorter alleles S_1 transmitted to the next generation in S_0S_1 heterozygote males is given by parameter d, ranging from d = 0.5(Mendelian segregation) to d = 1 (complete distortion). Fitness effects of the distorter are inspired by the t haplotype system in house mice, where -depending on the distorter type— S_1S_1 homozygotes suffer either from male sterility (sterile type) or lethality in both sexes (lethal type).

The life cycle

We consider an infinite population of diploids with nonoverlapping generations. Because males and females are differently affected by selection, we track their genotype frequencies independently. Let $X_{ij,kl,mn}$ denote female genotype frequencies, where ij defines status at the T locus, kl status at the P locus, and mn status at the distorter locus S. Analogously, male genotype frequencies are given by $Y_{op,qr,st}$. To derive the recursion equations for the resulting 64 ordered male and female genotypes, we assume the following life cycle.

We start our life cycle with the zygotes of the present generation. Analogous to above, the sex-independent genotype frequencies at the zygote stage are given by $Z_{ij,kl,mn}$. First, viability selection occurs. Viabilities are different in the two sexes (see Table 1). Females carrying P_1 alleles suffer from a fixed viability cost c_p (cost of preference). For simplicity, we assume that viability selection at the preference locus is additive (viability of P_0P_1 heterozygotes is $1-\frac{c_p}{2}$). Likewise, the male trait may come at a viability cost c_t . We assume that T_1T_1 homozygotes have a viability $1 - c_t$ while T_0T_1 heterozygote viability is given by $1 - h_t c_t$ (where h_t denotes the dominance coefficient). In the case of a distorter with homozygous lethal effects, S_1S_1 individuals have zero viability irrespective of sex. The resulting overall viabilities for males $w_{ij,kl,mn}$ and females $v_{ij,kl,mn}$ are then given as the product of the viability effects at each locus. Based on the zygote frequencies $Z_{ij,kl,mn}$, we can calculate the adult genotype frequencies:

$$X_{ij,kl,mn} = Z_{ij,kl,mn} \frac{v_{ij,kl,mn}}{\bar{v}}, Y_{op,qr,st} = Z_{ij,kl,mn} \frac{w_{ij,kl,mn}}{\bar{w}}, \quad (1)$$

where \bar{v} and \bar{w} denote mean female and male viability, respectively.

In the second step, adults of the present generation mate with each other. Females choose mates according to fixed relative preferences. This relative tendency of a female of P-genotype kl to mate with a male of T-genotype op is given by $a_{kl \times op}$ (see also Table 1). Parameters h_p and h_a describe dominance effects of preference, where h_p defines preference strength of P_0P_1 heterozygote females and h_a quantifies preference strength for heterozygote T_0T_1 males. The mating frequency between males of genotype op, qr, st and females of genotype ij, kl, mn is thus

$$F_{ij,kl,mn \times op,qr,st} = X_{ij,kl,mn} Y_{op,qr,st} \frac{a_{kl \times op}}{\overline{a_{op}}},$$
 (2)

where $\overline{a_{op}}$ is a normalizing constant that ensures that the fertility of a female does not depend on her mate choice.

Given the frequencies of the mating combinations from equation (2), we can now calculate the resulting zygote frequencies $Z'_{ii,kl,mn}$ of the next, nonoverlapping generation. Zygote frequencies will depend on segregation distortion d as well as on the recombination rate r_{UV} between loci U and V $(r_{TS}, r_{PS}, r_{TP},$ see Table S1). These recombination rates are not independent of each other, that is for a given combination of r_{TS} and r_{PS} , $r_{TP} = r_{TS} + r_{PS} - 2r_{TS}r_{PS}$. In the case of a sterile distorter, matings involving S_1S_1 males produce no offspring.

All results presented in this manuscript reflect numerical solutions of the system of recurrence equations. Distorter frequencies are usually empirically measured at the adult stage. Allele frequencies in this manuscript were hence recorded at the adult stage. At this stage, we also calculated the standardized linkage disequilibrium D'_{uv} between allele U_1 and V_1 (at frequencies u_1 and v_1) defined as (Lewontin 1964)

$$D'_{uv} = \frac{D_{uv}}{D_{max}} \quad \text{where} \quad D_{uv} = \{u_1 v_1\} - u_1 v_1 \quad \text{and}$$

$$D_{max} = \begin{cases} \min[u_0 v_1, u_1 v_0] & \text{if } D_{uv} \ge 0\\ \min[u_0 v_0, u_1 v_1] & \text{if } D_{uv} < 0. \end{cases}$$
(3)

Here, $\{u_1v_1\}$ denotes the frequency of U_1V_1 haplotypes among adult genotypes. For a more detailed description of the model, see Supplementary Text S1.

For most of the manuscript, we will consider a scenario where wild-type allele S_0 and the male signal T_1 are fully linked, that is $D'_{ts} = -1$ and $r_{TS} = 0$. This assumption will be relaxed for the last result section.

Results

EVOLUTION IN THE ABSENCE OF A DISTORTER

We begin our model analysis by considering sexual selection for a costly male trait in the absence of a distorter locus. The evolutionary outcome strongly depends on whether female preferences

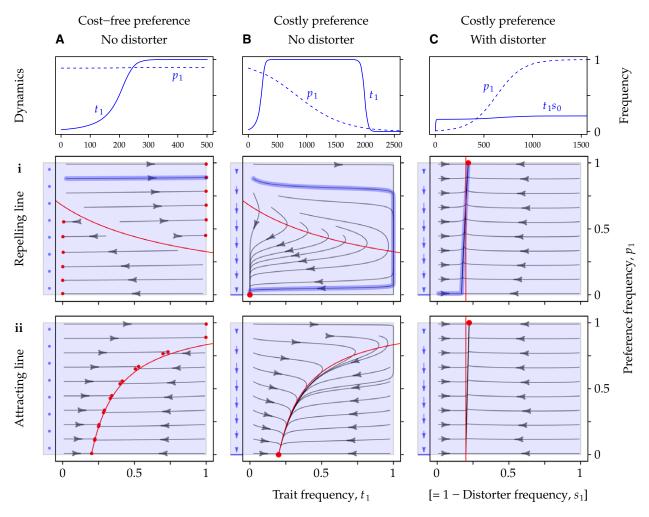


Figure 1. Joint evolution of trait t_1 and preference p_1 alleles in the absence (A–B) and presence (C) of a distorter. Center row panels (i) illustrate a scenario of a repelling line of quasi-equilibria, lower row panels (ii) a scenario an attracting line of quasi-equilibria (indicated by the red lines, based on Greenspoon and Otto (2009)). Top panels follow the allele frequency dynamics of a specific evolutionary trajectory of scenario (i) over time (shaded in blue). In A, the preference is cost-free (parameter values for scenario (i): a = 0.4, $h_a = 0.5$, $h_p = 0.3$, $p_c = 0$, $c_t = 0.15$, $h_t = 0.5$, $r_{PT} = 0.5$; parameter values for scenario (ii): a = 0.4, $h_a = 0.5$, $h_p = 0$, $p_c = 0$, p

are cost-free (Fig. 1A) or whether choosiness is associated with costs (Fig. 1B).

Evolution of cost-free preference

In the absence of a distorter, the evolution of cost-free female preferences ($c_p = 0$) has been studied in detail both numerically (Heisler and Curtsinger 1990) and analytically (Gomulkiewicz and Hastings 1990; Otto 1991; Greenspoon and Otto 2009). The evolutionary dynamics strongly resemble its haploid equivalent, Kirkpatrick's classical model of Fisherian sexual selection (Kuijper et al. 2012). Because there is no direct selection on the pref-

erence allele, p_1 evolves as a correlated response to changes at the trait locus (Fisher process). Evolution at the trait locus is determined by the interplay between natural selection (favoring allele T_0) and sexual selection (favoring allele T_1). Natural and sexual selection balance each other at points that form curves of quasi-equilibria in allele frequency space (the red curves in Fig. 1A); these curves correspond to the lines of equilibria in Kirkpatrick's haploid model (Greenspoon and Otto 2009). While the line of equilibria is always attracting under haploidy, curves of quasi-equilibria can either be repelling (Fig. 1Ai) or attracting (Fig. 1Aii) under diploidy, depending on whether the combination of natural

and sexual selection induces net underdominance or net overdominance at the male trait locus (Greenspoon and Otto 2009).

Evolution of costly preference—the lek paradox

Any female preference allele will eventually be selected against and disappear from the population if the slightest costs of choosiness are associated with this allele (Pomiankowski 1987). Both in the case of a repelling and an attracting curve of quasi-equilibria, evolution at the trait locus will eventually stop because one of the two alleles is fixed (case i) or the polymorphic equilibrium is reached (case ii). At this point, there are no indirect benefits of being choosy because the population is monomorphic at the male trait locus (problem i) or none of the male trait alleles are selectively favored (problem ii). As a consequence, even small choice costs induces selection against the preference allele and will push it to extinction (Fig. 1B). In the literature, this problem is known as the "lek paradox".

THE DISTORTER AS A TARGET OF FEMALE **PREFERENCES**

In the scenario considered above, a costly preference could not evolve because the system evolves to a state where the benefits of choosiness become negligible. The situation may be different if female preferences are targeted at a distorter allele. Distortion may help maintain trait variation despite directional sexual selection (problem i) and confer benefits to choosy females even if trait alleles are at a polymorphic equilibrium (problem ii).

It is unlikely that females base their mate choice directly at the males' genotype at the distorter locus. Instead, female preferences will be based on male traits that may convey information on the presence or absence of distorter alleles. Yet, we will postpone the analysis of such a three-locus scenario (distorter locus, trait locus, preference locus) and first consider the much simpler case where females can directly differentiate between distorter genotypes, or, equivalently, where the trait allele T_1 is in full linkage to the wildtype allele S_0 ($D'_{ts} = -1$) and no recombination between the Tand the S locus occurs ($r_{TS} = 0$). Thus, the model reduces to a diallelic 2-locus system, containing P_0 and P_1 alleles at the Plocus and T_1S_0 and T_0S_1 haplotypes at the trait/distorter locus (henceforth, we will refer to distorter frequency s_1 only, where $s_1 = t_0 = 1 - t_1$). Because T_1 alleles only occur together with the wild-type S_0 allele, a female that chooses a T_1 male will, at the same time, avoid the distorter allele S_1 .

We will first consider an illustrative example of mate choice targeted at a sterile distorter allele based on the parameter values of Fig. 1B. Next, we investigate systematically how evolutionary dynamics are affected by model parameters and the type of distorter. Finally, we explain the various outcomes by means of a simple intuitive argument. This will help us understand four qualitatively different evolutionary outcomes and their parameter dependence.

An illustrative example

We start with a situation where females avoid a distorter that is selectively neutral in females and induces sterility in males that are homozygous for the distorter (as in the case of the "sterile thaplotypes" in the house mouse, Lyon (1986)). The evolutionary dynamics of sterile, autosomal distorters in the absence of sexual selection ($P_1 = 0$) have been derived by Dunn and Levene (1961): the distorter is positively selected at the genetic level (segregation distortion) while counterselected at the organismic level (male sterility). The two forces balance at a stable, polymorphic equilibrium given by $\hat{s}_{p=0} = 2d - 1$ (see red vertical line Fig. 1C).

Figure 1C shows the evolutionary dynamics if the costly preference is targeted at a distorter. The parameter values are identical to the two scenarios in Fig. 1B, allowing us to directly compare the evolutionary outcome in the presence and absence of a distorter. The costly preference allele P_1 now rises to fixation, both in the repelling and attracting scenario. The two factors that previously inhibited the spread of costly preference are now avoided. Firstly, the distorter allele S_1 is not lost despite directional sexual selection against it (problem i, see Fig. 1B). Sexual selection against the distorter is counteracted by segregation distortion favoring the distorter. Note that selection for distorter alleles S_1 is particularly strong at low distorter frequencies (van Boven and Weissing 2001; Weissing and van Boven 2001). The resulting polymorphism prevents the lek paradox and fuels selection at the preference locus. Secondly, choice is beneficial even if the distorter frequencies are at the polymorphic equilibrium \hat{s} (problem ii, see Fig. 1B). Segregation distortion creates a situation where both S_1 and S_0 stably coexist, even though S_0S_0 , S_0S_1 , and S_1S_1 males dramatically differ in their individual fitness. The costly preference helps females to avoid the fitness costs of mating with a distorter-carrying male.

Dependence of preference frequency on model parameters

To systematically explore the parameter conditions that facilitate the evolution of a costly preference targeted at a distorter, we calculated evolutionary trajectories for systematically varying levels of preference strength a, preference cost c_p , and distortion strength d. Each model run was started with a low preference frequency $p_1 = 0.01$ and the distorter at equilibrium $(s_1 = \hat{s}_{p=0})$. With these starting conditions, we iterated the recurrence equations until allele frequencies reached equilibrium (\hat{p}_1, \hat{s}_1) , defined as the point where allele frequency changes became exceedingly small (Δp_1 and $\Delta s_1 < 10^{-8}$). For simplicity, we assume that trait costs are absent ($c_t = 0$) and females do not differentiate between S_0S_1 and S_1S_1 males ($h_a=0$), that is they avoid them with same probability (a).

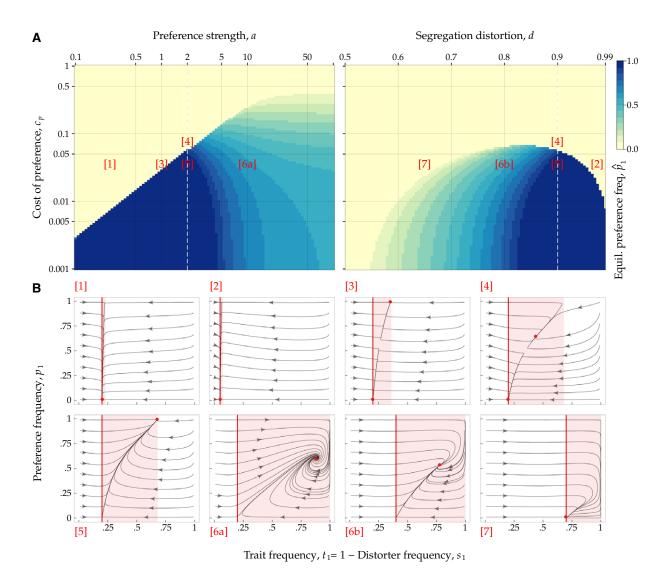


Figure 2. (A) Equilibrium preference frequencies \hat{p}_1 of a preference allele targeted at a sterile distorter in relation to preference strength (a), preference cost (c_p) and distorter strength (d). Preference strength a and cost c_p are shown on a \log_{10} -scale. The left panel is based on a distorter strength of d = 0.9, the right panel on a preference strength of a = 2, with the vertical dotted lines indicating the location where phase-plots intersect. Red numerals (1–7) depict parameter combinations that correspond to scenarios 1–7 that are schematically summarized in Figure 3 (scenario 6 occurs twice). (B) Evolutionary trajectories of distorter s_1 and preference p_1 alleles of the respective parameter combination/scenario. The red vertical line indicates the distorter equilibrium in the absence of preference $\hat{s}_{p=0}$. The red shaded area denotes the feasible distorter range. The red dots correspond to the end point of each evolutionary trajectory (~equilibrium). Remaining parameter values: $c_t = 0$, $h_p = 0.5$, $h_a = 0$, $r_{PS} = r_{PT} = 0.5$.

Equilibrium preference frequencies \hat{p}_1 as a function of a, c_p , and d are shown in Fig. 2A. Overall, the preference allele can invade and persist in a population for a large spectrum of the parameter space considered, if targeted at a sterile or lethal distorter (see Supplementary Text S1 for evolutionary outcomes if the distorter is lethal). In extreme cases, the preference allele can sustain preference costs as high as $c_p \approx 0.4$, that is a 40% viability reduction in choosy females. As one would expect intuitively, higher preference costs c_p invariably result in reduced preference frequency. Interestingly, both preference strength a and distortion strength a affect equilibrium preference frequencies in

a nonmonotonic fashion. Preference frequencies are highest at intermediate values of a and d. At low and high levels of a and d, the spread of a costly preference is typically limited.

A systematic analysis of parameter dependence

To intuitively understand the nonmonotonic relationship between model parameters and evolutionary outcomes (Fig. 2A), let us schematically examine two ranges of distorter frequency. Firstly, we specify the range of distorter frequencies that can be attained (at equilibrium) for varying frequencies of the preference allele, denoted as the "feasible distorter frequency

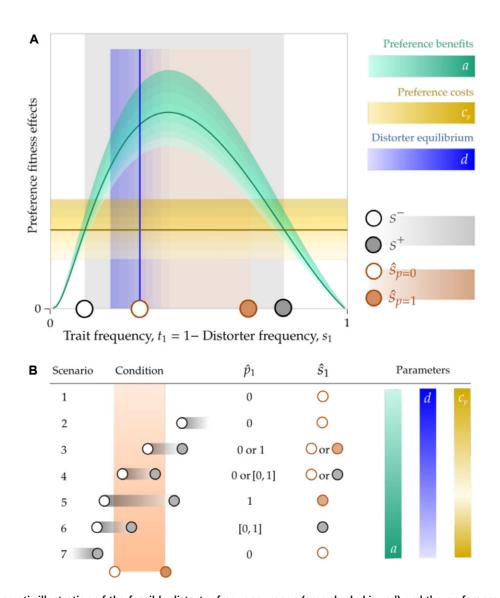


Figure 3. (A) Schematic illustration of the feasible distorter frequency range (area shaded in red) and the preference favoring distorter range (area shaded in grey) for intermediate levels of preference strength a, preference costs c_p , and distorter strength d (indicated by green, yellow, and blue lines, respectively, corresponding to scenario 5). The *feasible distorter range* corresponds to the spectrum of the distorter equilibria, ranging from the distorter equilibrium where preference is absent $\hat{s}_{p=0}$ (open red dot) to the distorter equilibrium where all females express a preference $\hat{s}_{p=1}$ (closed red dot). Parameter dependence: The blue shading illustrates how the position of $\hat{s}_{p=0}$ depends on the levels of distorter strength d (with darker shades representing higher d levels). The position of $\hat{s}_{p=1}$ will be a function of both preference and distorter strength a, d. The preference favoring distorter range specifies the distorter frequency spectrum where the preference allele is selectively favored, that is where preference benefits outweigh preference costs. Parameter dependent. Green shading illustrates the effect of preference costs levels c_p . Note that preference costs are distorter frequency independent. Green shading illustrate the effect of preference strength a. The points where the cost and benefit line intersect, that is where preference costs and benefits are in balance, correspond to unstable and stable preference equilibria s^- (open black dot) and s^+ (closed black dot), respectively. (B) Overview over the seven possible scenarios (as shown in Fig. 2), the four qualitatively different evolutionary outcomes (\hat{p}_1 , \hat{s}_1), and their parameter dependence. The "Condition" column schematically illustrates the relative position of the feasible distorter range and the preference favoring range (color coding corresponding to panel A).

range" $[\hat{s}_{p=0}, \hat{s}_{p=1}]$ (red shaded areas in Fig. 3). It falls between the distorter equilibrium where preference is absent $(\hat{s}_{p=0})$ and the distorter equilibrium where all females in a population are choosy $(\hat{s}_{p=1})$. Secondly, we specify the distorter frequency range for which the preference allele is selectively fa-

vored (i.e. where choice benefits outweigh costs), denoted as the "preference favoring distorter range" $[s^-, s^+]$. Preference costs, as implemented in the model, are distorter frequency independent (see yellow line in Fig. 3A). Preference benefits, on the other hand, crucially depend on distorter frequency: if the

distorter allele is absent ($s_1 = 0$) or fixed ($s_1 = 1$) a female will gain no benefits from choice. Intermediate distorter frequency confers highest benefits (see green line in Fig. 3A). As a result, the preference allele will only be selectively favored in the range $[s^-, s^+]$ (gray shaded area in Fig. 3). The points s^- and s^+ mark the unstable and stable preference equilibria, respectively, where preference costs and benefits are in balance.

Figure 3 schematically illustrates the two ranges and how model parameters affect their size and position. The feasible distorter range and preference favoring range can be arranged in seven different ways (scenario 1-7) that correspond to four qualitatively distinct evolutionary outcomes. The evolution of the costly preference allele is limited whenever the feasible distorter frequencies fall outside the preference favoring range.

If preference strength is very small or distortion is strong, preference costs either outweigh benefits for all distorter frequencies (scenario 1, Fig. 2[1]) or the preference favoring range falls completely outside the feasible distorter range (scenario 2, Fig. 2[2]), and the preference allele is lost. At intermediate preference and distorter strength, feasible distorter frequencies are most likely to overlap (at least partly) with the preference favoring range, thereby creating conditions most favorable for costly choice evolution. If the unstable equilibrium point s^- falls inside the feasible distorter range, evolutionary trajectories will depend on whether distorter frequency falls above or below s^- , resulting in a bistable system with two equilibrium points (scenarios 3 and 4, Fig. 2[3] and [4]). If the costly choice is favored for all feasible distorter frequencies, it will rise to fixation irrespective of starting frequency (scenario 5, Fig. 2[5]). Interestingly, very strong preferences (and weak distorters) also limit the costly preference evolution, because effective choice typically drive distorters close to extinction, at which point costly choice no longer returns net benefits (as was the case in "lek paradox" scenarios in the absence of a distorter). The result is either the extinction of the preference (scenario 7, Fig. 2[7]) or damped oscillatory dynamics around stable equilibrium s^+ (scenario 6, Fig. 2[6a,b]). In scenario 6, female choice pushes distorter frequencies close to extinction where preference benefits are marginal, which results in a decrease of preference levels. This decrease will, in turn, weaken sexual selection against distorters, allowing S_1 alleles to increase once again, and the cycle starts anew.

RECOMBINATION BETWEEN THE MALE SIGNAL AND THE DISTORTER

So far, we have assumed full linkage between the trait and the distorter locus, thus effectively considering a two-locus system where the distorter allele is a direct target of female mate choice. While this assumption may be realistic for some distorter systems (Williams and Lenington 1993), potential male signals may be more loosely coupled to the distorter in others (e.g., in stalk-eyed

flies). Analyzing the full complexity of the three-locus model is a daunting task. We therefore restricted our analysis to a simpler question: How do the results of the previous section change if we introduce a low level of recombination between the trait locus T and the distorter locus S (i.e., r_{TS})? To this end, we started at the equilibrium in full linkage $(D'_{ts} = -1)$ and considered the subsequent evolution of the system for a small but positive value of r_{TS} . We find that preference alleles disappear from the population already at minimal levels of recombination ($r_{TS} = 10^{-3}$, see Fig. S1). Recombination will rapidly produce an increasing number of T_1S_1 haplotypes that are favored both by sexual selection and distortion. Because choosy females increasingly mate with distorter carrying males, female choice will no longer confer fitness benefits and thus be lost. We examined all parameter combinations shown in Fig. 2 in this manner, and find that conclusion is representative for the whole parameter space explored in this study. Hence, the successful evolution of the costly preference breaks down even at very low recombination rates between the male trait and the distorter.

Discussion

We have demonstrated that female choice for distorter-free males can spread and persist in a population even if mate choice is associated with considerable direct fitness costs. This is in contrast to classical models of sexual selection where preference costs typically result in the loss of female preference (Kuijper et al. 2012). Two key components of the distorter enable spread and maintenance of the costly female choice allele. The spread is a consequence of the large benefits associated with avoiding carriers of distorter alleles. The maintenance results from the fact that segregation distortion helps preserve male trait variation despite directional sexual selection. The balance of gene-level selection in favor and individual-level selection against the distorter alleles keeps allele frequencies at the distorter locus in a firm polymorphic state, thus avoiding the lek paradox that often hampers the maintenance of costly mate choice. Akin to previous resolutions (Kotiaho et al. 2008), the present model proposes a mechanism (distortion) that maintains trait variation in the face of directional sexual selection. Our model has also identified several factors that limit the evolution of the costly preference allele. Interestingly, we find that preference evolution is limited if the distorter is very strong or if the preference allele induces strong preferences. In the latter case, the lek paradox prevails. Moreover, we show that the costly preference can only spread in the presence of a signal that reliably indicates a male's distorter genotype. Accordingly, already the smallest degree of recombination between a male signal and the distorter will result in the disappearance of the costly preference.

Our findings are consistent with the few previous models addressing mate choice evolution in the presence of distorters, all focusing on different types of sex-linked distorters (Lande and Wilkinson 1999; Reinhold et al. 1999; Randerson et al. 2000). In the case of sex-linked distortion, choice benefits stem from the fact that mating with a distorter-free partner will result in offspring of even sex ratio. Since the sex ratio of populations harboring sexlinked distorters is strongly biased, producing offspring of the rarer sex conveys a selective advantage as individuals of the rarer sex have a higher reproductive value (Pen and Weissing 2001). The conclusions are similar to the ones presented here: cost-free (Lande and Wilkinson 1999) and costly (Randerson et al. 2000) mate choice for distorter/male-killer-free mates can stably persist. Mate choice for drive suppression, on the other hand, seems not beneficial (Reinhold et al. 1999). Despite these similarities, there may be quantitative differences between autosomal and sex-linked distorters.

Reliable indicators of distortion

Preference benefits of female choice are only guaranteed if the male trait is a reliable indicator of the genetic status at the distorter locus. In line with Lande and Wilkinson (1999), we found that even small recombination rates between trait and distorter inhibit the spread of the choice allele as they erode the reliability of the signal and hence benefits of choice. Given this restrictive prerequisite, one may conclude that our model can explain the presence of a costly preference for distorter-free mates in only few real-world systems. Full linkage between a sexually selected trait and a distorter is possible if recombination between the loci is suppressed or the distorter itself is the signal (i.e., the signal is a pleiotropic effect of the distorter). A scenario where the distorter itself is the target of female mate choice could be given if the distorter directly affects the phenotype, for example by reducing the overall condition of its carriers. Although most distorters known to date have no or little effects on the external phenotype (Burt and Trivers 2006), it is feasible that genomic methods will help us detect distorters (weak distorters in particular, see last paragraph) that directly affect condition. Such variance in male condition could then serve as a basis for mate choice on condition-dependent traits.

Alternatively, the trait "recognizable" to females can be fully linked to a distorter due to a lack of recombination. Interestingly, suppression of recombination is an essential part of distorter systems as the effects of segregation distortion hinge upon the interaction of several genes (but also see van Boven and Weissing (2000)). In fact, recombination has been proposed as a way for an organism to avoid selfish action of groups of linked genes by decoupling possible alliances (Leigh 1971). Hence what makes a distorter effective in the first place, suppression of recombination, may render them at the same time vulnerable to negative sexual selection. Through the lack of recombination, there is a chance that the distorter will be bound to a gene with phenotypic

effects recognizable to females, thereby allowing mate choice against it. The t haplotype in house mice, for example, consists of about 300 genes linked to each other through four chromosomal inversions (Burt and Trivers 2006). Among these genes are several major histocompatibility complex (MHC) loci, that have been proposed as signals mediating mate choice (Milinski 2006). In a study on a wild house mouse population, Lindholm et al. (2013) have shown that t haplotypes were associated with a unique and exclusive MHC allele. There is mixed evidence for mate choice in the t haplotype system. It has been detected in some (Lenington et al. 1992), but not all populations (Manser et al. 2015; Sutter and Lindholm 2016), and the role of MHC remains controversial (Lenington et al. 1988). To date, there is relatively limited evidence for mating preferences in connection with distorters (Wilkinson et al. 1998; Wedell 2013; Price et al. 2012), but this may be due to the limited data. Price et al. (2012) have explicitly tested for precopulatory avoidance of distorter males in *Drosophila pseudoobscura* but did not find any evidence in a series of lab experiments. The requirement of a signal accidentally trapped in the distorter's linkage group may explain why premating choice is relatively rare (but see last section).

Another female strategy to avoid fertilization by distortercarrying males that has been relatively widely discussed is polyandry and subsequent sperm competition. The genetic mechanisms underlying segregation distortion typically result in lower sperm number and/or lower sperm quality. As a result, distortercarrying males are often compromised in their sperm competitive ability (Price and Wedell 2008). Females may capitalize on this fact by mating with multiple males (polyandry), thereby avoiding fertilization by distorter-males (Haig and Bergstrom 1995). This is interesting in the context of the model presented here, because the phenotype causing nonrandom fertilization, reduced sperm competitiveness, is a pleiotropic effect of the distorter itself. As a result, no suppression of recombination between a signal and the distorter is needed for the evolution of polyandry. Although not investigated explicitly, our model may thus indirectly explain why empirical evidence for polyandry as a female counterstrategy against distorters is far more abundant than premating choice. In a recent study, Holman et al. (2015) investigated this scenario in the context of a sex-linked distorter. Akin to the results presented here, they found that polyandry can evolve and be stably maintained if the distorter is stabilized at an intermediate frequency by negative frequency dependent selection. Further studies are required to investigate whether their findings translate to autosomal distortion systems.

Maintaining distorters alleles

Our model demonstrates that a costly mate choice can only successfully evolve if distorter frequencies are kept at intermediate frequencies, where the preference allele is selectively favored. The successful spread of the preference allele is hence the result of a delicate balancing act. Any selective force that pushes distorter frequencies to one or the other extreme of the distorter frequency spectrum will limit the evolution of costly choice. Accordingly, we found that very strong or weak levels of segregation distortion hamper the spread of the preference allele. Similarly, a costly mate choice can only be maintained efficiently if the preference is of intermediate strength. If directional sexual selection is strong, it may override the distorter's capacity to create new male trait variance. In this case, the lek paradox prevails. Once choosy females have successfully removed most distorters from the population, that is male variation has expired, preference costs again start to outweigh preference benefits, just as in our original scenario without a distorter (where already marginal levels of preference are sufficient to run into that problem, see Fig. 1B). Preference frequency will then stabilize at a lower level that allows for enough male trait variation to keep benefits and costs of choice in balance (scenario 6). In other words, costly mate choice for Mendelian segregation will only escape the lek problem in a given spectrum of preference strength. At the lower end of the spectrum, choice is not effective and benefits of choice are hence limited. At the upper end of the spectrum, sexual selection is—once more— too strong to maintain male trait variation. It is unclear if the levels of preference strength needed for this second effect are biologically relevant. However, the question about which levels of preference strength would evolve if they were allowed to vary freely is an interesting theoretical question in itself, especially considering the non-straightforward relationship between preference strength and equilibrium preference frequency.

Does mate choice suppress distorter frequencies?

So far, we have largely focused on the distorter's influence on the sexual selection process. However, we can also ask how costly female choice affects distorter dynamics. Accounting for distorter frequencies in wild populations is a long standing focus of evolutionary theory (Burt and Trivers 2006). Depending on its strength, female mate choice may be an important determinant of distorter frequency (e.g., Manser et al. (2011)). Akin to molecular suppressors of distortion proposed elsewhere, female mate choice can be seen as a behavioral mechanism to reduce drive frequency by creating selection against individuals that carry a distorter. By undermining the spread of the selfish distorter, female choice may help to maintain harmony at the genomic level. However, our current model suggests that this mechanism will only be successful to a certain degree, at least as long as female choice is costly and drift effects are negligible. The scenario where the lek paradox prevails as a consequence of strong directional sexual selection (scenario 2) makes clear that female choice will never completely remove the distorter. As soon as mate choice is effective in removing distorter alleles, benefits of choice fade, allowing the distorter back in. Intriguingly, this may provide an explanation for a problem known as the low t frequency paradox in house mice. In the t haplotype system in house mice, t frequencies in wild populations are usually at low (lower than expected from distortion and lethality only) but stable levels (Ardlie 1998; van Boven and Weissing 1999). Costly female choice may explain why t frequencies are lower than expected, yet stably prevail in populations.

Practical implications for artificial distorters

The role of mate choice in suppressing distorter frequencies has also potential practical implications. Recently, distorter systems have sparked great interest as potential tools to control disease vectors, agricultural pests, and invasive species (Sinkins and Gould 2006). Rapid advances in genome editing technology not only allow us to synthesize genes with desirable characteristics for human ends, but, when paired with a segregation distorter, such constructs could also be released to sweep through natural target populations (Galizi et al. 2014). For example, the male determining gene Sry is currently being inserted in the t haplotype region of house mice. Males carrying such a t-Sry construct will result in 90% male offspring, and could thus be used to control or eradicate invasive mouse populations for conservation purposes (Piaggio et al. 2017). House mice are extremely damaging to the ecosystems as invasives, in particular to endemic fauna on islands. We still have very limited knowledge of what would happen if such constructs are released into natural populations. Although not modeled explicitly, our work suggests that sexual selection against t-Sry males could potentially render a release ineffective (a point made previously by Gemmell and Tompkins (2017)). The fact that, additional to the t lethal effect, the construct renders females sterile and results in male-biased offspring (thereby increasing the fitness cost to a female mating with a t-Sry male) will certainly increase the selective pressure on females to avoid males that carry the artificial distorter. Moreover, as sex ratios become increasingly male biased, competition over reproduction among males and thus the opportunity for sexually selective processes is likely to intensify.

A general mechanism for the evolution of costly mate choice?

The presented model demonstrates that segregation distorters can greatly facilitate the evolution of female choice, even if such a choice is associated with substantial fitness costs. We can only speculate about the importance of distorter systems for the evolution of female choice in general. Selfish genetic elements are considered a ubiquitous feature of life (Burt and Trivers 2006). However, the abundance of autosomal distorter systems considered here, particularly among animals, is largely unknown. The covert action of distorters make detection and identification inherently difficult. It is not surprising that the best known

distorter systems were both found in two of the best-studied model organisms (t haplotype in the house mouse and Segregation Distorter in Drosophila). Deviations from Mendelian inheritance are occasionally reported in other species, but the causes of such biased inheritance is often unknown (Burt and Trivers 2006). In both known cases, segregation distortion is relatively effective $(d \approx 0.9)$. It is not known whether this feature is representative of distorter systems in general or whether it is the result of a detection bias (as weaker distorters are more difficult to discover). Our model suggests that a weak distorter's capacity to promote female mate choice is reduced, because weak distortion easily results in distorter equilibria outside the preference favoring range (scenarios 6 and 7). However, if not only distortion is weaker, but also its selective effects on the organism (here, distorters result in male sterility or homozygote lethality), distorter equilibria may well shift back into the preference favorable range. In any case, the present model shows the action of distorters, usually hidden from sight, may play an important role in driving the evolution of costly female choice.

AUTHOR CONTRIBUTIONS

AM, FJW, and AKL conceived of the modelling idea. AM and FJW developed and analysed the model. AM, FJW, and AKL wrote the manuscript.

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DATA ARCHIVING

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Supporting Information

Additional Supporting Information may be found in the online version of this article at the publisher's website:

Figure S1. Equilibrium preference frequencies \hat{p}_1 of a preference allele targeted at a lethal distorter in relation to preference strength (a), preference cost (c_p) and distorter strength (d).

Figure S2. Disappearance of female preference for fair Mendelian segregation as a result of recombination between the trait and the distorter locus.

Table S1. Gametes produced by each male genotype as a function of segregation distortion d as well as recombination between the loci, r_{TS} and r_{SP} .